

Maxwell equations:

$$D = \epsilon_0 E + P = \epsilon \epsilon_0 E$$

$$B = \mu_0 (H + M)$$

$$\nabla \cdot B = 0$$

$$\nabla \cdot D = \rho_{free(non-dipole)}$$

$$\nabla \cdot (\epsilon - 1) \epsilon_0 D = \rho_{dipole}$$

$$\nabla \times H = J + \frac{\partial D}{\partial t}$$

$$\nabla \times E + \frac{\partial B}{\partial t} = 0$$

Solid-State Electronics

Equation of motion of carriers in solid:

$$\frac{d\vec{p}}{dt} + \frac{\vec{p}}{\tau} = \vec{F} = -e(\mathbf{E} + \mathbf{v} \times \mathbf{B}), \text{ where } \mathbf{p} = m\mathbf{v}$$

$$\mathbf{v} = \frac{q\mathbf{E}}{m} \tau, \text{ or } \mu = \frac{q}{m} \tau$$

where q is the charge ($-e$ for electron)

Boltzmann Transport Equation

$$\frac{df}{dt} = -\mathbf{v} \cdot \nabla f - \mathbf{F} \cdot \nabla_p f + \left(\frac{\partial f}{\partial t} \right)_{collision}$$

where $f(x, v, t)$ is the distribution function and \mathbf{F} is the force field.

Shockley Equations for semiconductors:

$$q \frac{\partial n}{\partial t} = \nabla \cdot j_n + q(g_n - r_n)$$

$$q \frac{\partial p}{\partial t} = -\nabla \cdot j_p + q(g_p - r_p)$$

$$j_n = q\mu_n nE + qD_n \nabla n = n\mu_n \nabla E_{Fn}$$

$$j_p = q\mu_p pE - qD_p \nabla p = p\mu_p \nabla E_{Fp}$$

$$\nabla \cdot \epsilon E = \rho = q(p - n + N_D^+ - N_A^-)$$

$$\frac{\partial n_T}{\partial t} = (g_p - r_p) - (g_n - r_n)$$

Mechanical beam equation

$D\nabla^4 y + T\nabla^2 y = \rho d^2 y/dt^2$, where ρ is the mass per unit area.

Energy Transfer Equations (first law of thermal dynamics):

$$\rho c_p \frac{dT}{dt} = k\nabla^2 T + \mu\Phi + \ddot{q}$$

$$\ddot{q} = -k\nabla T$$

where $\mu\Phi$ is viscous dissipation (kinetic energy \rightarrow heat) and \ddot{q} is internal heat generation and \dot{q} is the heat flux.

Navier Stokes equations:

$$\rho \frac{d\mathbf{u}}{dt} = -\nabla p + \mu\nabla^2 \mathbf{u} + \mathbf{F}$$

μ the dynamic viscosity ($\nu = \mu/\rho$, the kinematic viscosity).

Continuity Equation:

$$\frac{d\rho}{dt} + \rho\nabla \cdot \mathbf{u} = 0$$

Plasma as a fluid:

$$mn \left[\frac{\partial \mathbf{u}}{\partial t} + (\mathbf{u} \cdot \nabla) \mathbf{u} \right] = \text{total force} = qn(\mathbf{E} + \mathbf{u} \times \mathbf{B}) - \nabla p - \frac{mn(\mathbf{u} - \mathbf{u}_0)}{\tau} + \rho\nu\nabla^2 \mathbf{u} + mngh$$

$$p = C\rho^\gamma \text{ or } p = nKT$$

$$\frac{\partial n}{\partial t} + \nabla \cdot (n\mathbf{u}) = 0$$

(convective derivative) of momentum = Lorentz force + pressure-collision + viscous damping + gravitation.